

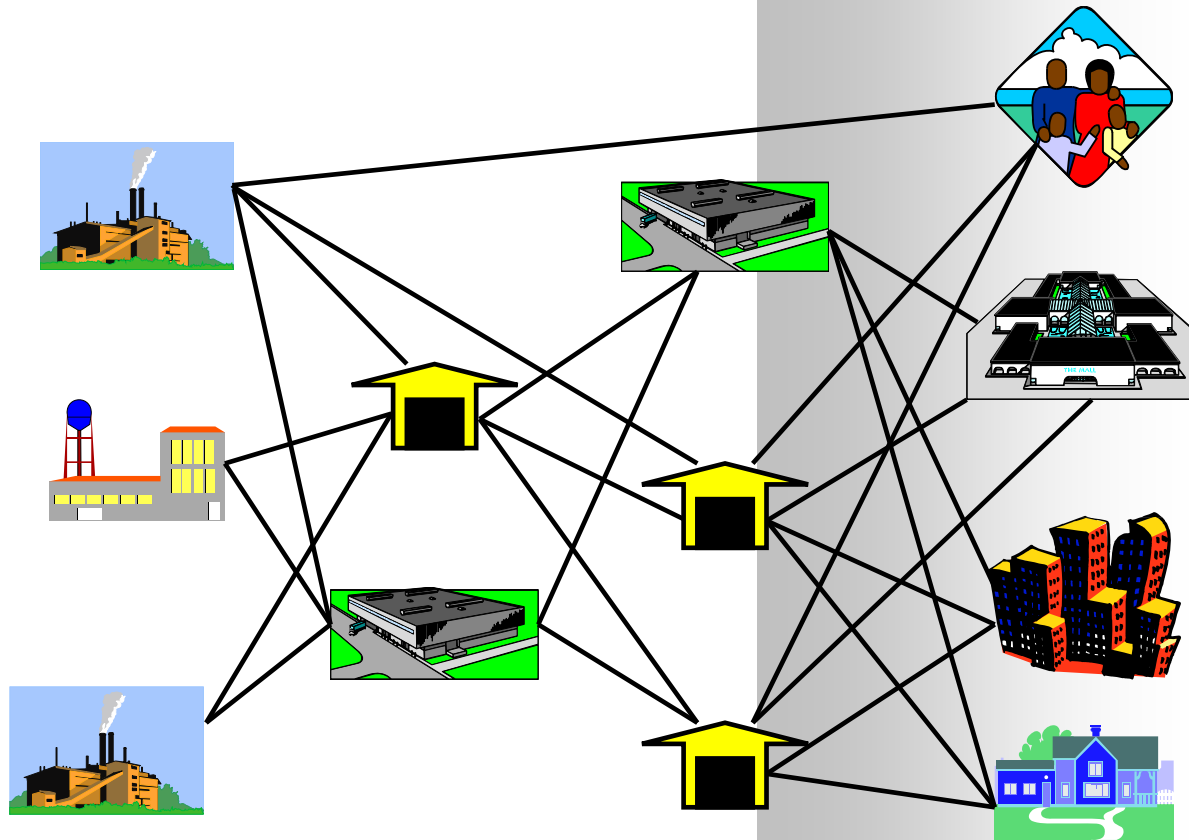
# Operations Research in Supply Chain Optimization

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November 12, 2010

# The supply chain



Suppliers → factories → warehouses → customers

## Goal of supply chain management

To efficiently integrate suppliers, producers, warehouses to produce and distribute

- the right quantity
- at the right time
- in the right place

*Operations Research*

while maximizing the total profit and guaranteeing an appropriate service level

## Goal of supply chain management

- All strategies, techniques, approaches in supply chain management are focused on:

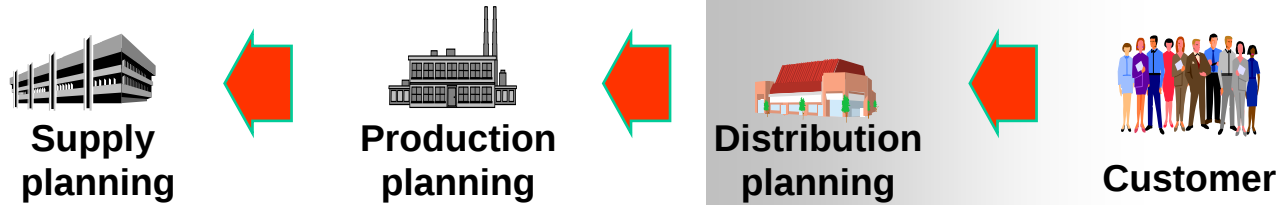
- Global optimization

- Uncertainty management

*Operations Research*

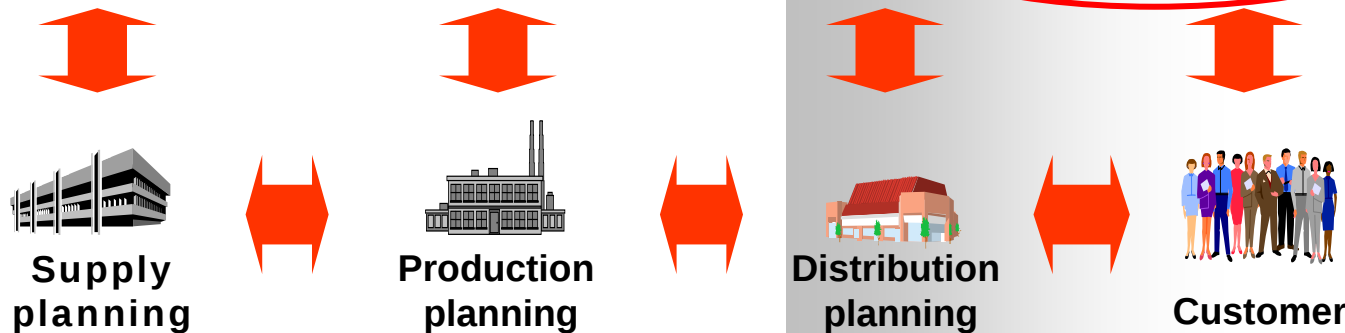
# Global optimization

## Sequential optimization



## Global optimization

Contracts – collaboration – Information technology – **Decision Support Systems**



*Operations Research*

## Global optimization

- Search process of the best strategy for the entire supply chain to:

*Operations Research*

maximize overall value created

- Supply chain value: difference between what the final product is worth to the customer and the effort the supply chain expends in filling the customer's request

## Why is it difficult?

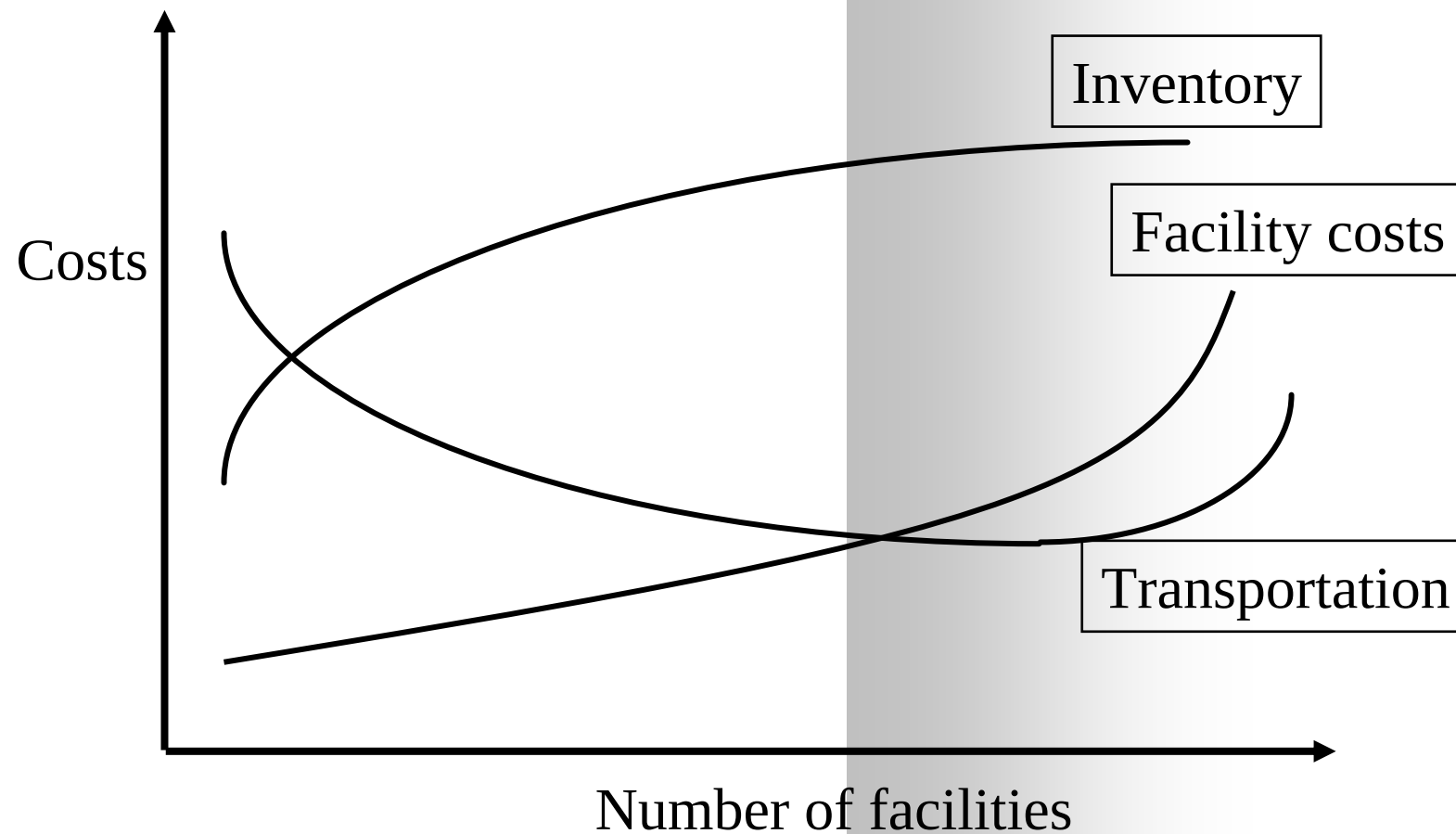
- The supply chain is complex
- The different actors have different goals
- The supply chain evolves upon time
- The system varies (changes, demand, costs)



*Operations Research*

A need of sophisticated tools,  
models, algorithms

## An example of complexity



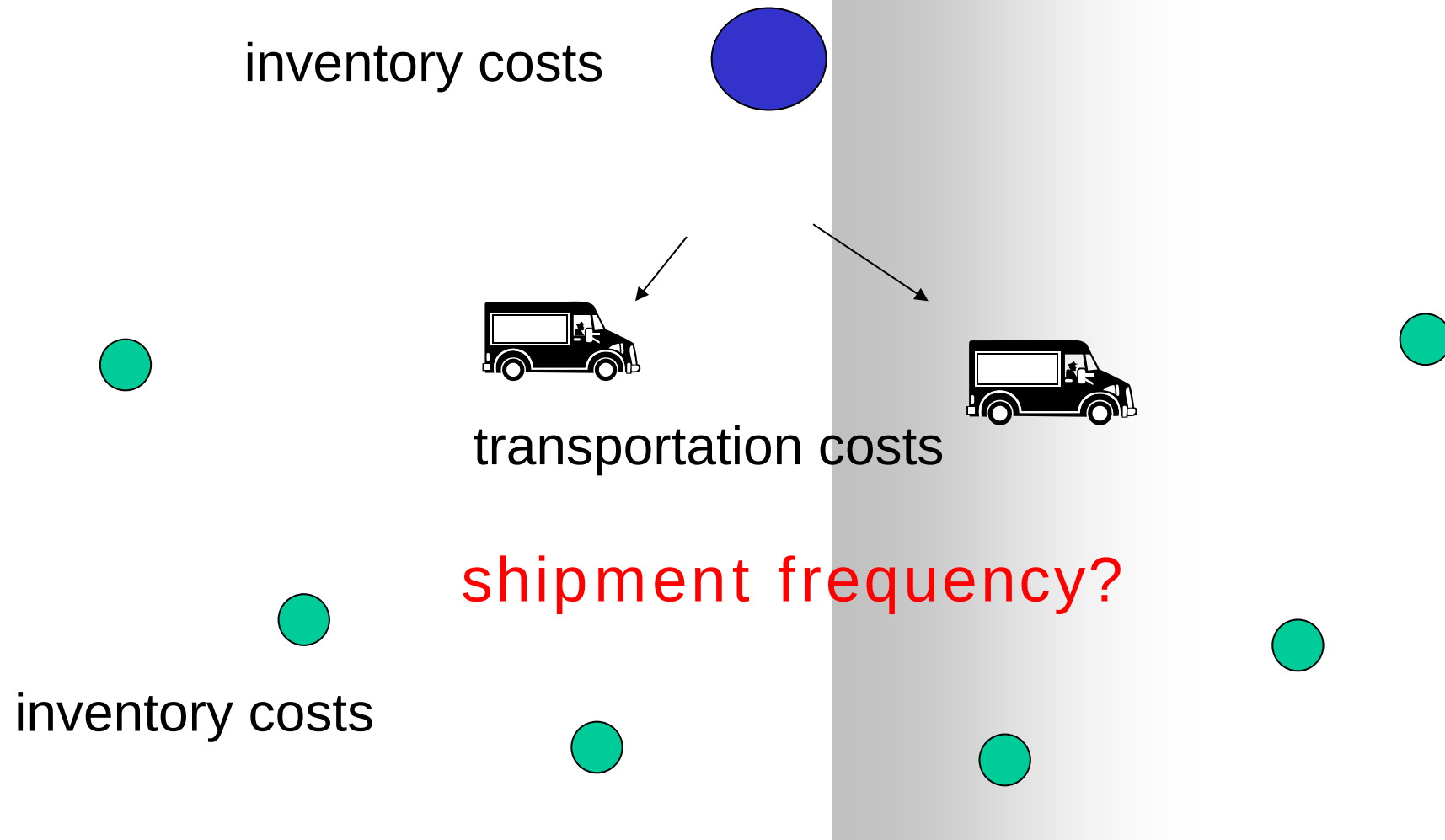
## Conflicting objectives

- Lot Size – Inventory
- Inventory – Transportation
- Lead Time – Transportation
- Product Variety – Inventory
- Cost – Customer Service

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# A distribution network



# Conflicting objectives

Main reason for infrequent (full load) transportation:  
minimize transportation costs

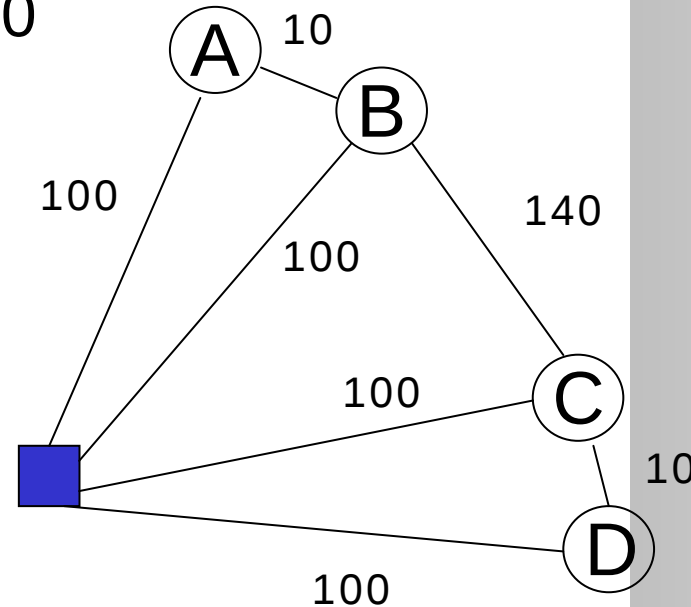
Main reason for frequent transportation:  
minimize inventory costs

Problem: Minimize transportation or inventory costs?

Minimize the sum of inventory and transportation costs

# The value of integration

1 vehicle  
capacity 100

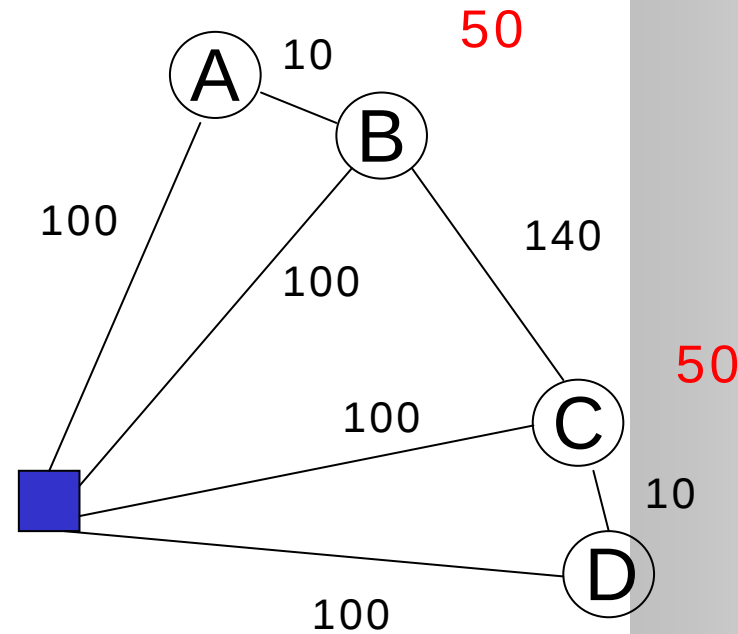


frequency of service  
is every 2 days

customers decide when and how much  
supplier decides routes

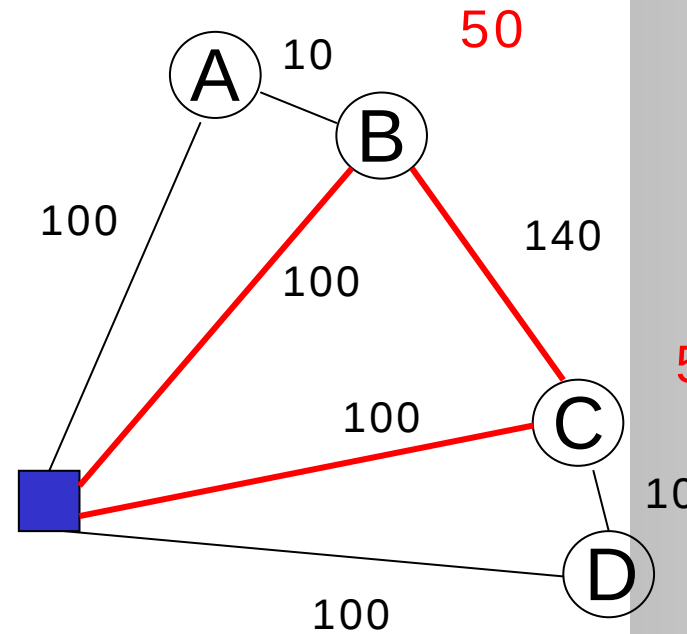
# The value of integration

Day 1



# The value of integration

Day 1



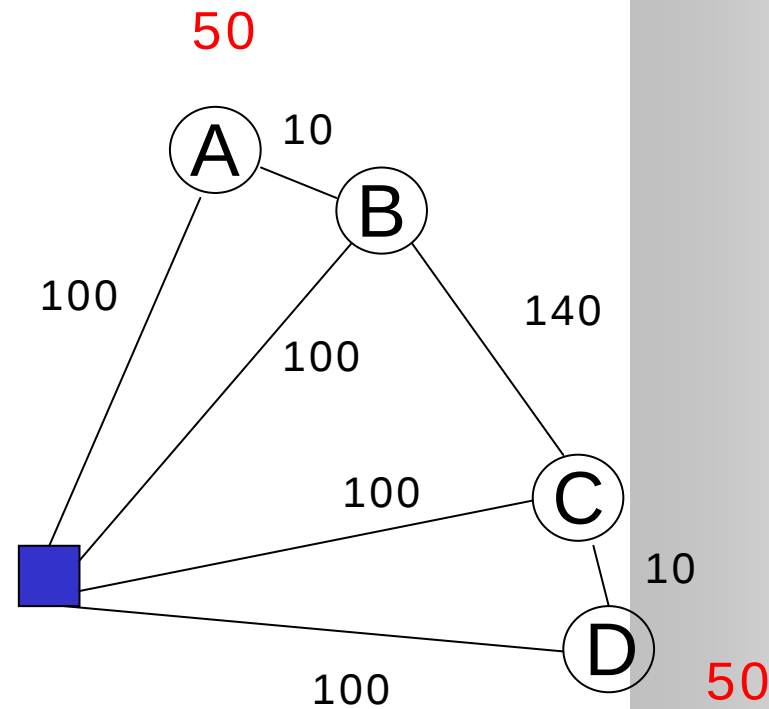
50



Cost = 340

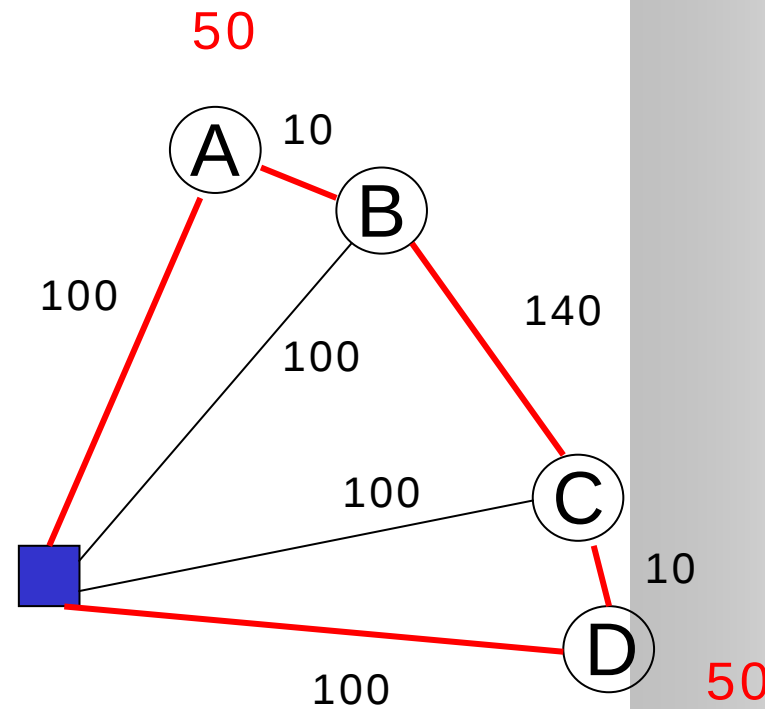
# The value of integration

Day 2



# The value of integration

Day 2

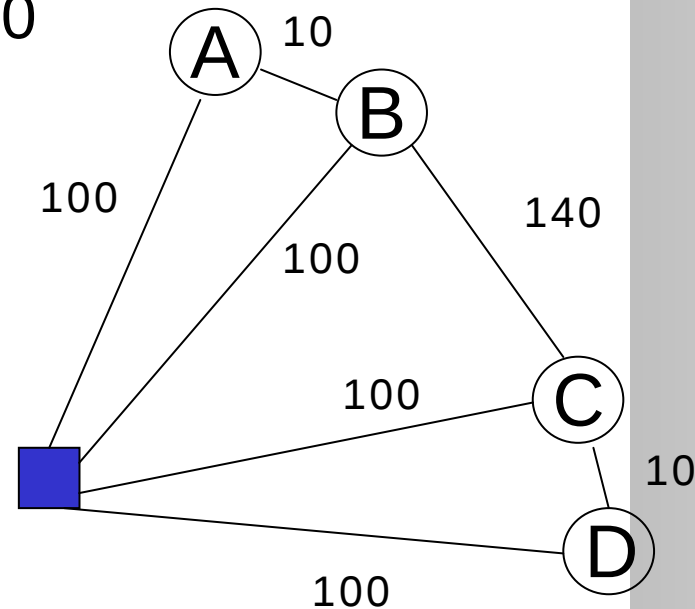


Cost = 360

Cost over two days = 700

# The value of integration

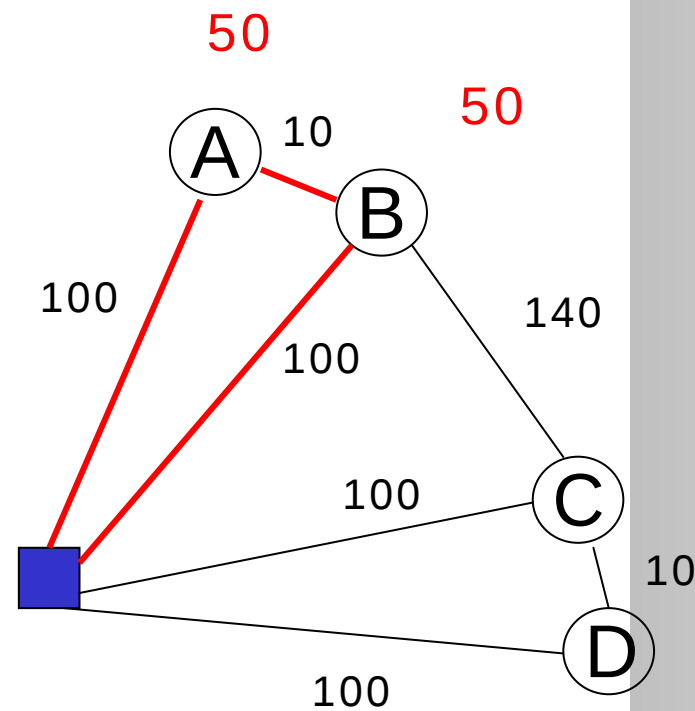
1 vehicle  
capacity 100



supplier decides when, how much and routes

# The value of integration

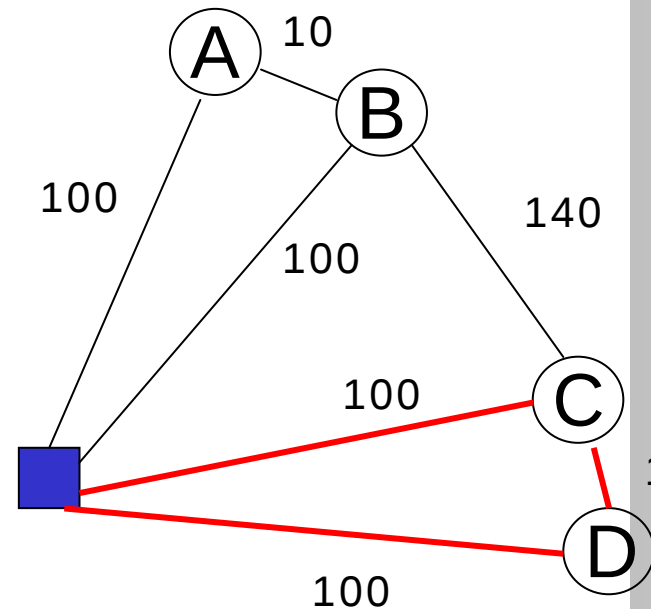
Day 1



Cost = 210

# The value of integration

Day 2



50



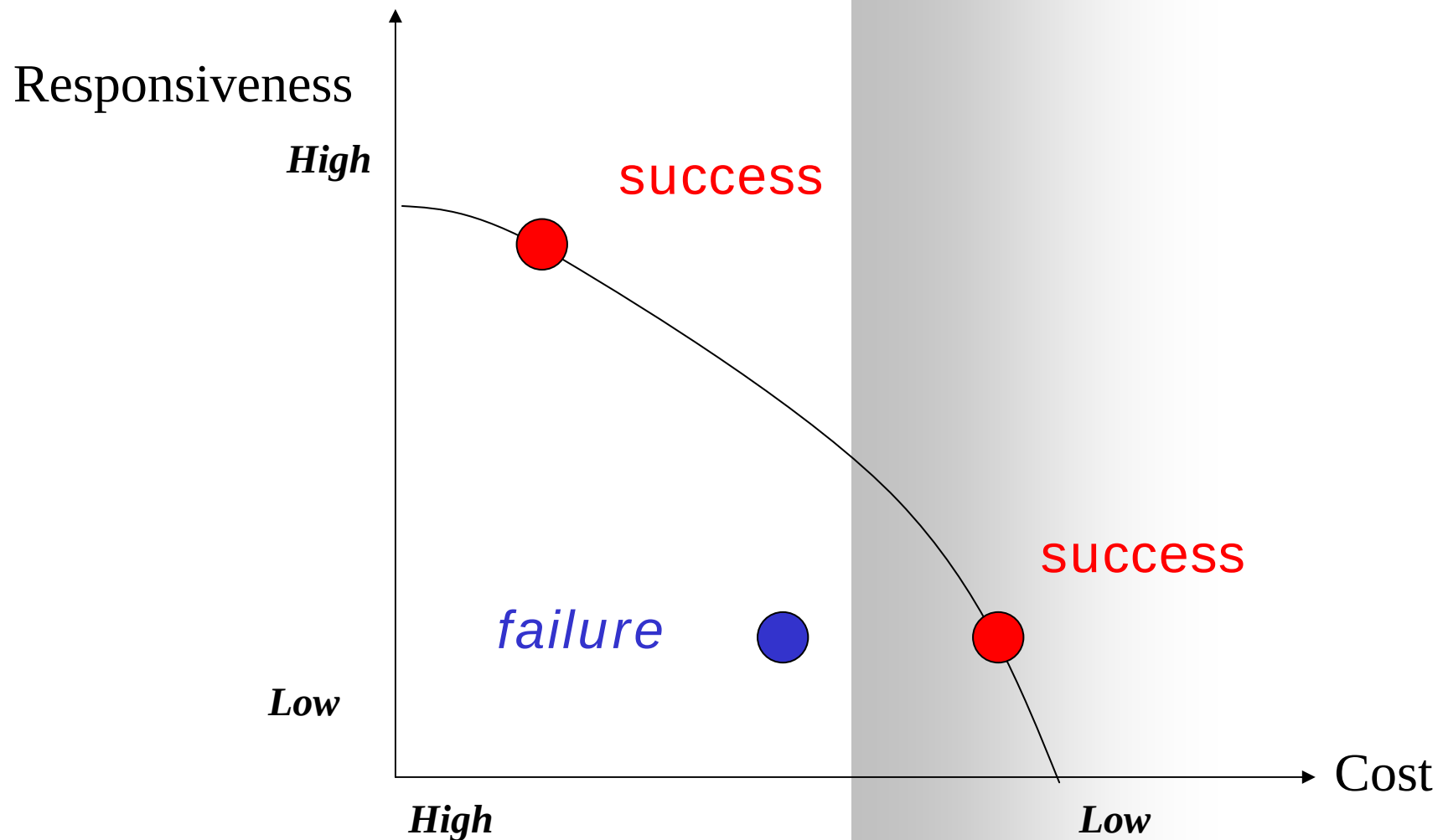
Cost = 210

10

50

Cost over two days = 420  
(against 700)

# Efficient frontier



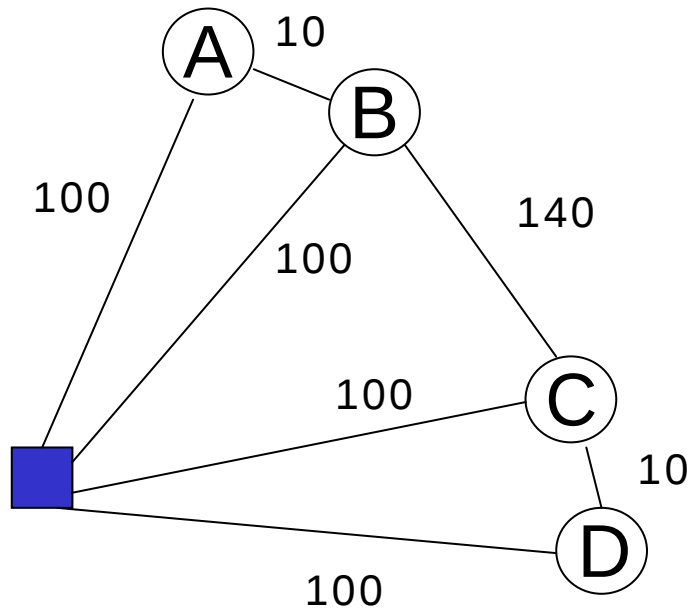
# Efficiency and complexity

In global competition companies  
need to be on the efficient frontier

Intuition fails to generate efficient  
management policies

Need for integration and efficiency  
makes decision making more complex

# Optimal policy



|   |  | capacity | demand |
|---|--|----------|--------|
| A |  | 5000     | 1000   |
| B |  | 3000     | 3000   |
| C |  | 2000     | 2000   |
| D |  | 4000     | 1500   |

Initial inventory=capacity

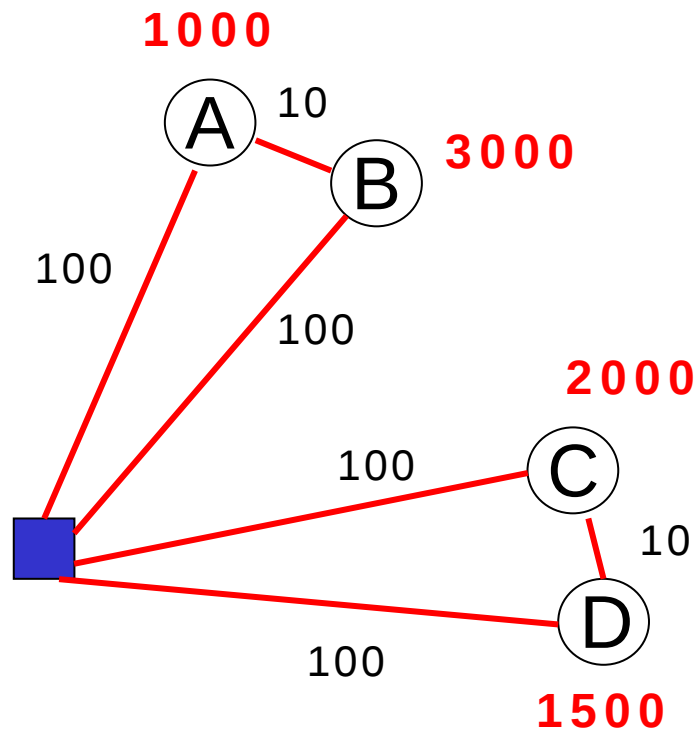
The supplier has unlimited availability

Capacity of vehicles 5000

? Periodic policy of minimum  
transportation cost

*Bell et al (1983), Interfaces*

## A natural solution

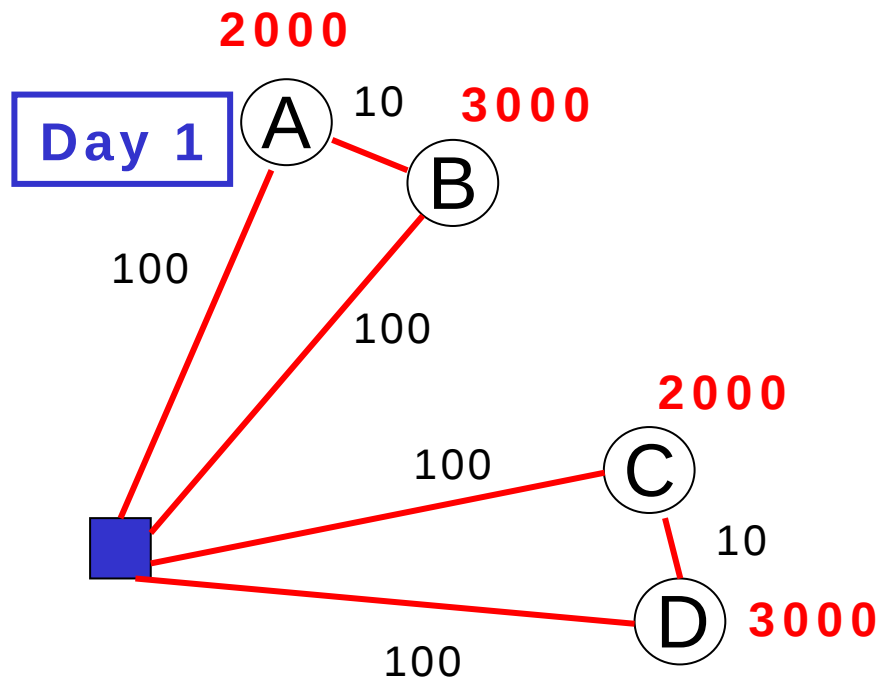


|   |  | capacity | demand |
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| A |  | 5000     | 1000   |
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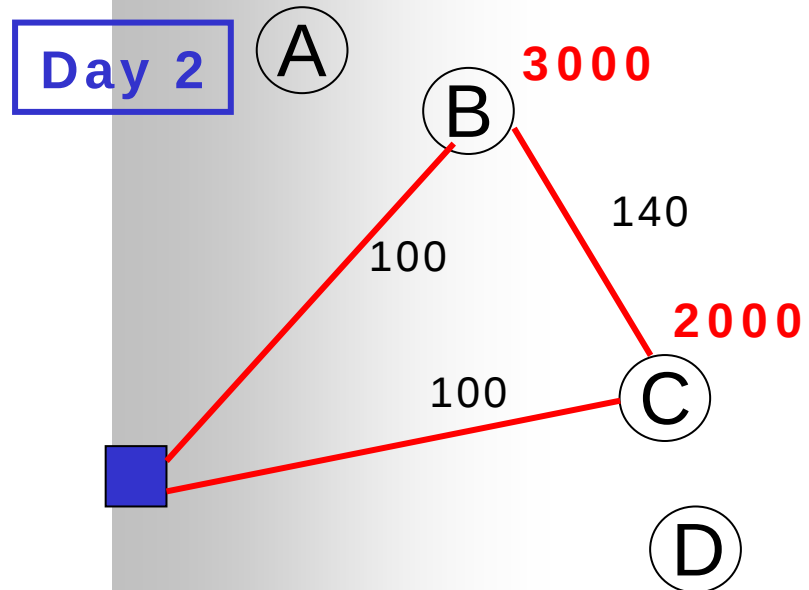
2 vehicles

Repeat the red and the green tours every day  
Daily transportation cost: 420

## A better solution

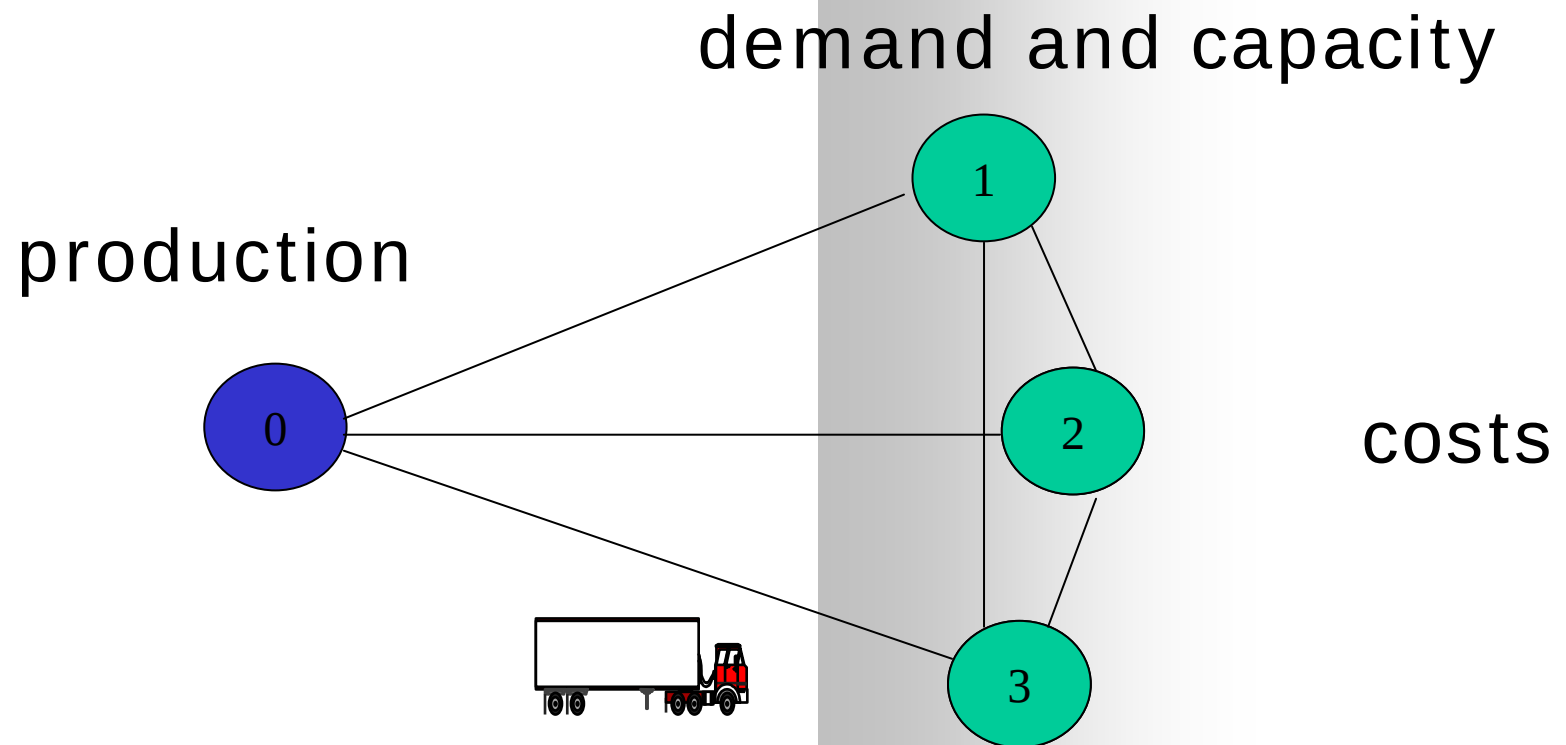


|   | capacity | consumption |
|---|----------|-------------|
| A | 5000     | 1000        |
| B | 3000     | 3000        |
| C | 2000     | 2000        |
| D | 4000     | 1500        |

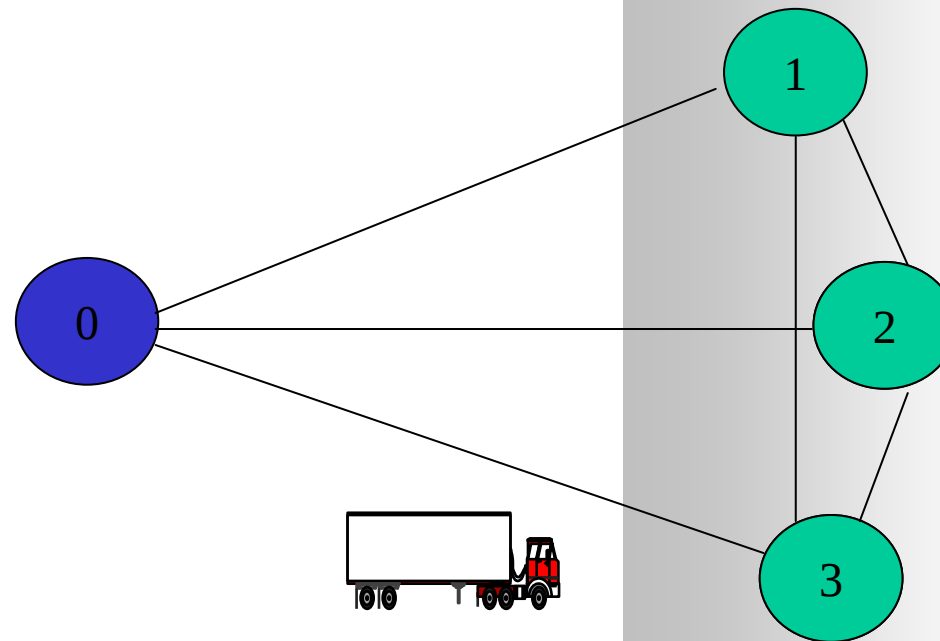


Average daily  
transportation cost: 380

# An integrated problem



# An integrated problem



When and how much to produce?  
When and how much to distribute?  
Routes?  
Goal: to minimize total cost

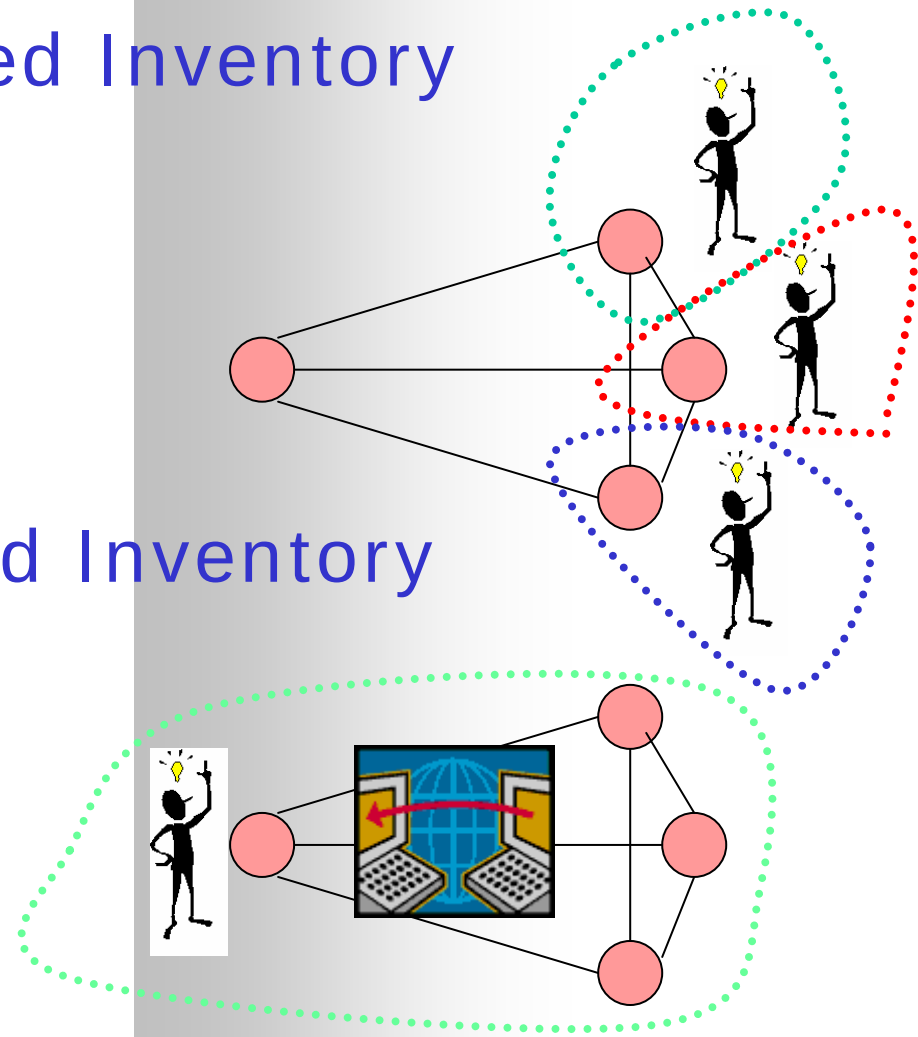
# RMI vs VMI

## ➤ RMI: Retailer-Managed Inventory

Each retailer decides its replenishment policy

## ➤ VMI: Vendor-Managed Inventory

The supplier monitors the inventory level of each retailer and decides the replenishment policy of each retailer



## VMI vs RMI – the OU policy

|                                    | VMI<br>Order-up |
|------------------------------------|-----------------|
| general case                       | 71%             |
| no fixed<br>transportation<br>cost | 92%             |
| small<br>production<br>cost        | 50%             |
| no retailer<br>inventory cost      | 67%             |

Cost of VMI with respect to RMI

## VMI vs RMI – the OU policy

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Cost of VMI with respect to RMI

# Conclusions

- Integrated models are very complex
- Large savings can be achieved
- Appropriate models and algorithms (Operations research) are essential